

# Determination of accurate rest frequencies and hyperfine structure parameters of cyanobutadiyne, HC<sub>5</sub>N

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## Abstract

Very accurate transition frequencies of HC<sub>5</sub>N were determined between 5.3 and 21.4 GHz with a Fourier transform microwave spectrometer. The molecules were generated by passing a mixture of HC<sub>3</sub>N and C<sub>2</sub>H<sub>2</sub> highly diluted in neon through a discharge valve followed by supersonic expansion into the Fabry-Perot cavity of the spectrometer. The accuracies of the data permitted us to improve the experimental <sup>14</sup>N nuclear quadrupole coupling parameter considerably and the first experimental determination of the <sup>14</sup>N nuclear spin-rotation parameter. The transition frequencies are also well suited to determine in astronomical observations the local speed of rest velocities in molecular clouds with high fidelity. The same setup was used to study HC<sub>7</sub>N, albeit with modest improvement of the experimental <sup>14</sup>N nuclear quadrupole coupling parameter. Quantum chemical calculations were carried out to determine <sup>14</sup>N nuclear quadrupole and spin-rotation coupling parameters of HC<sub>5</sub>N, HC<sub>7</sub>N, and related molecules. These calculations included evaluation of vibrational and relativistic corrections to the non-relativistic equilibrium quadrupole coupling parameters; their considerations improved the agreement between calculated and experimental values substantially.

## Keywords:

microwave spectroscopy, interstellar molecule, cyanopolynes, hyperfine structure, quantum chemical calculation

## 1. Introduction

Cyanopolynes H(C≡C)<sub>n</sub>CN occur abundantly in space, in particular the shorter members. Molecules up to cyanooctatrayne, HC<sub>9</sub>N ( $n = 4$ ), were detected [1]. The next longer member, HC<sub>11</sub>N, has not yet been found in space [2]. Isotopic species with D or with one <sup>13</sup>C were detected up to HC<sub>7</sub>N [3], <sup>15</sup>N isotopologs up to HC<sub>5</sub>N [4], even all three isotopomers of HC<sub>3</sub>N with two <sup>13</sup>C were observed astronomically [5]. Measurements of the HC<sub>3</sub>N species and the isotopomers with one <sup>13</sup>C were frequently used to determine <sup>12</sup>C/<sup>13</sup>C ratios in various objects, such as the protoplanetary nebula CRL618 [6, 7] or in starless cores, where differences in the <sup>12</sup>C/<sup>13</sup>C ratios were found [8].

Cyanobutadiyne, HC<sub>5</sub>N, also known as cyanodiacetylene or pentadienenitrile, was detected as early as 1976 toward the high-mass star-forming region Sagittarius B2 close to the Galactic center [9]. It was found soon thereafter in the dark and dense core Heile's Cloud 2 [10], nowadays better known as Taurus Molecular Cloud 1 or short as TMC-1 [11]. Cyanohexatriyne, HC<sub>7</sub>N, also known as cyanotriacetylene or heptatriene-nitrile, was discovered in that source [12]. Both molecules were

also found early in the circumstellar envelope of the famous carbon rich asymptotic giant branch star CW Leonis, also referred to as IRC+10216 [13].

Molecules up to HC<sub>17</sub>N ( $n = 8$ ) were investigated by rotational spectroscopy [14]. Alexander et al. were the first to investigate the rotational spectrum of HC<sub>5</sub>N [15]. They assigned ground state rotational spectra of eight isotopic species in the microwave (MW) region from which they determined structural parameters. They also determined the <sup>14</sup>N nuclear quadrupole coupling parameter  $eQq(N)$  and the dipole moment of the main isotopic species. Winnewisser et al. improved  $eQq(N)$  [16] and expanded the assignments into the millimeter wave (mmW) region [17]. Bizzocchi et al. recorded the spectra of HC<sub>5</sub>N and DC<sub>5</sub>N in the mmW and sub-mmW regions [18]. Assignments for these two isotopologs were extended to 460 GHz. They also analyzed spectra of singly substituted isotopic variants of both isotopologs containing one <sup>13</sup>C or <sup>15</sup>N, and derived from the rotational parameters a semi-experimental equilibrium structure.

Kirby et al. analyzed the ground state rotational spectrum of HC<sub>7</sub>N in the MW region [19]. McCarthy et al. subjected the main isotopic species as well as all singly substituted ones to a Fourier transform (FT) MW spectroscopic study and determined  $eQq(N)$  for all of them [20]. Similar studies were carried out for HC<sub>9</sub>N and HC<sub>11</sub>N, and ground state effective structural parameters for all three molecules. Soon thereafter, Bizzocchi et al. extended the assignments of the main isotopic species in its ground and several low-lying vibrational states into the

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mmW region [21].

The aim of the present work is twofold. The first target was the improvement of the hyperfine structure (HFS) parameters of  $\text{HC}_5\text{N}$  and potentially of  $\text{HC}_7\text{N}$ , and secondly, we wanted to investigate how accurately HFS parameters can be evaluated by high-level quantum-chemical calculations, and in particular trends among related molecules. An earlier study of isotopic species associated with  $\text{DC}_3\text{N}$  showed that very good agreement can be achieved for the nuclear quadrupole parameters in high-accuracy coupled-cluster calculations by employing large basis sets together with vibrational corrections [22].

## 2. Experimental details

Spectra between 5 and 22 GHz were recorded at the Leibniz-Universität in Hannover employing a supersonic-jet Fourier transform microwave (FTMW) spectrometer [23] in the coaxially oriented beam-resonator arrangement (COBRA) [24] which combines a very sensitive setup with an electric discharge nozzle [25]. Cyanobutadiyne was generated by passing a mixture of equal amounts of 1%  $\text{HC}_3\text{N}$  in neon and 1%  $\text{C}_2\text{H}_2$  in neon at a pressure of  $\sim 100$  kPa through the discharge nozzle and expanding the products into the cavity of the spectrometer. Cyanohexatriyne was obtained initially by the same procedure and subsequently by modifying the ratio of diluted  $\text{HC}_3\text{N}$  and  $\text{C}_2\text{H}_2$  from 1 : 1 to 1 : 2. Uncertainties of frequencies of 0.3 kHz and below can be achieved under favorable conditions [26, 27].

## 3. Observed spectra and determination of spectroscopic parameters

Prediction of the microwave spectra of  $\text{HC}_5\text{N}$  and  $\text{HC}_7\text{N}$  were very reliable based on earlier data [16, 18, 20, 21]. Pickett’s SPCAT and SPFIT programs [28] were used for prediction and fitting of the spectra, respectively. Each rotational level of  $\text{HC}_5\text{N}$  and  $\text{HC}_7\text{N}$  with  $J > 0$  is split by spin coupling effects caused by the  $^{14}\text{N}$  nucleus ( $I = 1$ ) into three HFS components. The rotational and spin angular momenta are coupled sequentially:  $\mathbf{J} + \mathbf{I}(^{14}\text{N}) = \mathbf{F}$ . At higher values of  $J$ , the strong HFS components are the ones conserving the spin orientation, i. e. those with  $\Delta F = \Delta J$ . The very narrow linewidths of a few kilohertz for an isolated line permits the corresponding HFS components to be resolved for all investigated transitions of  $\text{HC}_5\text{N}$  and  $\text{HC}_7\text{N}$ . However, the high sensitivity of the present  $\text{HC}_5\text{N}$  data allowed us to observe the weaker spin-reorienting HFS components with  $\Delta F = 0$  for all transitions and the even weaker ones with  $\Delta F = -\Delta J$  for the lowest two transitions ( $J = 2 - 1$  and  $3 - 2$ ). The transition frequencies obtained in the present investigation are summarized in Table 1 together with their quantum number assignments, uncertainties, and differences between experimental frequencies and those calculated from the global fit. The signal-to-noise ratios (S/N) of the spectral recordings of  $\text{HC}_5\text{N}$  were very high such that almost all lines were accurate to 0.2 kHz ( $1\sigma$ ), see also Refs 26, 27.

The very high quality of the  $\text{HC}_5\text{N}$  data prompted us to try to improve the data situation also for  $\text{HC}_7\text{N}$ . We recorded first data

Table 1: Rotational transitions of  $\text{HC}_5\text{N}$  with quantum numbers  $J$  and  $F$  recorded in the present study, their frequencies (MHz), uncertainties Unc. (kHz), residuals O–C (kHz) between observed transition frequencies and those calculated from the global fit.

$J' - J''$	$F' - F''$	Frequency	Unc.	O–C
2 – 1	2 – 2	5324.04642	0.20	0.05
	1 – 0	5324.26054	0.20	–0.06
	2 – 1	5325.32957	0.20	–0.24
	3 – 2	5325.42182	0.20	0.03
	1 – 2	5326.18468	0.20	0.20
3 – 2	1 – 1	5327.46808	0.20	0.16
	3 – 3	7986.61752	0.20	0.03
	2 – 1	7987.77870	0.20	0.02
	3 – 2	7987.99286	0.20	–0.05
	4 – 3	7988.04414	0.20	0.00
	2 – 3	7988.54163	0.20	0.27
4 – 3	2 – 2	7989.91689	0.20	0.11
	4 – 4	10649.22745	0.20	0.27
	3 – 2	10650.56191	0.20	0.06
	4 – 3	10650.65418	0.20	0.34
	5 – 4	10650.68658	0.20	0.04
5 – 4	3 – 3	10652.48571	0.20	–0.02
	5 – 5	13311.85257	0.20	0.06
	4 – 3	13313.26074	0.20	0.10
	5 – 4	13313.31208	0.20	0.21
	6 – 5	13313.33461	0.20	0.00
6 – 5	4 – 4	13315.09264	0.20	0.11
	6 – 6	15974.48392	0.20	–0.29
	5 – 4	15975.93351	0.20	–0.08
	6 – 5	15975.96655	0.20	0.25
	7 – 6	15975.98302	0.20	–0.03
7 – 6	5 – 5	15977.71410	0.20	–0.15
	7 – 7	18637.11750	0.20	–0.05
	6 – 5	18638.59378	0.20	0.12
	7 – 6	18638.61629	0.20	–0.10
	8 – 7	18638.62933	0.20	0.06
8 – 7	6 – 6	18640.34150	0.20	–0.11
	8 – 8	21299.74993	0.50	0.23
	7 – 6	21301.24497	0.20	0.30
	8 – 7	21301.26134	0.20	–0.08
	9 – 8	21301.27125	0.20	–0.40
	7 – 7	21302.96959	0.20	–0.30

Table 2: Rotational transitions of HC<sub>7</sub>N with quantum numbers  $J$  and  $F$  recorded in the present study, their frequencies (MHz), uncertainties Unc. (kHz), residuals O–C (kHz) between observed transition frequencies and those calculated from the global fit.

$J' - J''$	$F' - F''$	Frequency	Unc.	O–C
5 – 4	4 – 3	5639.9580	1.0	–0.12
	5 – 4	5640.0104	1.0	1.19
	6 – 5	5640.0325	1.0	0.72
6 – 5	5 – 4	6767.9778	1.0	0.38
	6 – 5	6768.0107	1.0	0.72
	7 – 6	6768.0261	1.0	–0.47
12 – 11	11 – 10	13535.9917	1.0	–0.54
	12 – 11	13535.9978	1.0	–1.21
	13 – 12	13536.0055	1.0	1.61

for the  $J = 12 - 11$  and  $6 - 5$  transitions which had been studied earlier [20]. The S/N were considerably lower than in the case of HC<sub>5</sub>N, as was expected. Therefore, only the  $\Delta F = \Delta J$  HFS components were detected with reasonable S/N even after long integration. In addition to remeasure transition frequencies of these two transitions, we recorded the  $J = 5 - 4$  transition at 5640 MHz, which was the lowest in frequency available at that time. The HC<sub>7</sub>N transition frequencies obtained in the present study are given with additional information in Table 2. The accuracies were 1 kHz ( $1\sigma$ ) in all instances.

Our present HC<sub>5</sub>N and HC<sub>7</sub>N data were fit together with previous data. Since the number of spectroscopic parameters is small with respect to the total number of lines of each molecule, the quality of the reproduction of the lines of each source is a good indication for the accuracies of the lines. These were 10 kHz for the hyperfine free MW center frequencies from Alexander et al. [15] and 7 kHz for the mmW data from Winnewisser et al. [17] and for the mmW and sub-mmW data from Bizzocchi et al. [18] in the case of HC<sub>5</sub>N. The accuracies were 1 kHz for the MW transition frequencies with HFS splitting from McCarthy et al. [20] and 10 kHz for those without HFS splitting in the MW region from Kirby et al. [19] and those in the mmW region from Bizzocchi et al. [21] for the HC<sub>7</sub>N molecule. The resulting spectroscopic parameters of HC<sub>5</sub>N and HC<sub>7</sub>N are given in Table 3 together with the most recent previous data.

The line lists and spectroscopic parameters are available as supplementary material to this article; the line, parameter, and fit files along with additional files are deposited in the data section of the Cologne Database for Molecular Spectroscopy<sup>2</sup> [29].

The large body of very accurate HC<sub>5</sub>N transition frequencies from the present study not only led to an improvement in  $eQq(N)$  by more than two orders of magnitude but also resulted in a very well determined value for the nuclear magnetic spin-rotation coupling parameter  $C$ , the coefficient of **I·J**. In addition, the uncertainties of  $B$  and  $D$  got reduced; the correlation of these parameters with  $H$  is likely responsible for the improve-

ment in the accuracy of  $H$ . The differences in the uncertainties of  $eQq(N)$  for HC<sub>7</sub>N between present and previous data are modest; and we should point out that part of the improvement is caused by assigning an uncertainty of 1 kHz to the earlier FTMW data [20] whereas 2 kHz were reported initially. The nuclear spin-rotation parameter  $C$  could not be determined for HC<sub>7</sub>N, therefore, it was kept fixed to the value determined in a quantum chemical calculation. This treatment led to a change in  $eQq(N)$  from  $-4.299 \pm 0.050$  MHz to  $-4.275 \pm 0.050$  MHz. The smaller uncertainty in the earlier  $B$  value [21] is caused by the fact that in that work unsplit (i.e. HFS free) transition frequencies were derived for the FTMW data [20] to which much smaller effective uncertainties were assigned. A more detailed discussion of the HFS parameters is presented in section 6.

#### 4. Application in astronomical observations

Emission lines of HC<sub>5</sub>N may be prominent in dense cold molecular clouds such as TMC-1 [30]. Therefore, the very accurate rest frequencies from this and previous studies may be used to determine the local speed of rest in such a cloud with great accuracy, even more so as transitions occur with a spacing of  $\sim 2660$  MHz and because the <sup>14</sup>N HFS splitting is usually resolved at low values of  $J$ . Table 4 lists some molecules which are often abundant in dense molecular clouds and have an at least moderately dense rotational spectrum and rest frequencies known very accurately at least in part. HC<sub>3</sub>N in its ground vibrational and low-lying vibrational states [31] or its isotopomers with one <sup>13</sup>C [32] or with D [22] have larger rotational spacings, but may be used over a much wider frequency and rotational temperature ranges. The same applies to propyne [33] and methyl cyanide [34, 35, 36]. Carbonyl sulfide [37, 38] can be quite abundant in dense parts of molecular clouds. Sulfur dioxide is more suited for spectra of hot cores and hot corinos, the warm and dense parts of high- and low-mass star-forming regions, respectively. Its rotational spectrum [39, 40, 41, 42] was also employed to calibrate rotational spectra of, e.g., H<sub>2</sub>CS [43, 44]. Methanol is very abundant in many different types of molecular clouds, but most reported transition frequencies have accuracies in the range of 50 kHz to 200 kHz; only limited data are available with better accuracies [40, 45, 46].

#### 5. Quantum chemical calculations

Calculations for the equilibrium structure as well as the <sup>14</sup>N nuclear quadrupole and spin-rotation coupling parameters were performed at the coupled-cluster (CC) level [47] using the coupled-cluster singles and doubles (CCSD) approach augmented by a perturbative treatment of triple excitations (CCSD(T)) [48, 49, 50, 51] together with correlation consistent core-polarized valence (cc-pCVXZ, X = T, Q, 5, 6) [52, 53, 54] basis sets. In the calculations of the spin-rotation tensors, perturbation-dependent basis functions, as described in Ref. [55, 56], were used to ensure fast basis-set convergence.

Molecular equilibrium structures were obtained at the CCSD(T)/cc-pCVQZ level of theory, which was shown to

<sup>2</sup>Webaddress: <https://cdms.astro.uni-koeln.de/classic/predictions/daten/>

Table 3: Ground state spectroscopic parameters<sup>a</sup> (MHz) of HC<sub>5</sub>N and HC<sub>7</sub>N in comparison to the most recent previous data.

Parameter	HC <sub>5</sub> N		HC <sub>7</sub> N	
	present	previous <sup>b</sup>	present	previous <sup>c</sup>
$B$	1331.332691 (4)	1331.332687 (20)	564.0011226 (75)	564.0011225 (44)
$D \times 10^6$	30.1099 (8)	30.1090 (15)	4.04117 (55)	4.04108 (54)
$H \times 10^{12}$	1.642 (19)	1.635 (29)	0.163 (10)	0.163 (10)
$eQq(\text{N})$	-4.27680 (14)	-4.242 (30)	-4.275 (50)	-4.29 (16)
$C \times 10^3$	0.2896 (123)		0.123	

<sup>a</sup> Numbers in parentheses are one standard deviation in units of the least significant figures. The parameter  $C$  of HC<sub>7</sub>N was kept fixed to the value of a quantum chemical calculation.

<sup>b</sup>  $B, D, H$  from Ref. [18];  $eQq(\text{N})$  from Ref. [16].

<sup>c</sup>  $B, D, H$  from Ref. [21];  $eQq(\text{N})$  from Ref. [20].

Table 4: Molecular species with a rich rotational spectrum suitable to determine the local speed of rest with high precision, approximate upper frequency  $\nu$  (GHz) for a certain accuracy, approximate accuracy Acc. (kHz) and references Ref. and comments.

Molecule	$\nu$	Acc.	Ref. and comments
HC <sub>5</sub> N	22	0.2	This work.
HC <sub>5</sub> N	500	7	[18] and references therein.
HC <sub>3</sub> N	120	1.0	[31].
HC <sub>3</sub> N	900	10	[31] and references therein; including several excited states.
HC <sub>3</sub> N	620	10–20	[32]; isotopic species with <sup>13</sup> C.
CH <sub>3</sub> CCH	720	0.5	[33]; $K \leq 12$ .
CH <sub>3</sub> CN	800	1.0	[34]; $K \leq 12$ .
CH <sub>3</sub> CN	1500	20–30	[35]; $v_8 \leq 2, K + l \leq 12$ .
CH <sub>3</sub> CN	1200	20–50	[36]; isotopic species with <sup>13</sup> C, $K \leq 9$ .
OCS	520	1.0	[37, 38]; better than 0.1 kHz for several lines.
SO <sub>2</sub>	120	2.0	[39, 40, 41]; $v_2 \leq 1$ , also $v = 0$ of <sup>34</sup> SO <sub>2</sub> , many lines.
SO <sub>2</sub>	2000	10–30	[42]; $v_2 \leq 1$ , several lines; many better than 50 kHz.
CH <sub>3</sub> OH	120	1–10	[40, 45, 46] and references therein; selected lines, possibly up to 200 GHz.

yield molecular equilibrium structural parameters of very high quality for molecules carrying first-row atoms [57], which applies as well for the HCN [57] and HC<sub>3</sub>N [22] systems studied here. Following the extensive basis set study presented in Ref. [22] for the equilibrium structure and the nuclear quadrupole as well as spin-rotation coupling parameters of HC<sub>3</sub>N (and DC<sub>3</sub>N) we apply a similar procedure here. The <sup>14</sup>N nuclear quadrupole coupling parameters of HCN, HC<sub>3</sub>N, DC<sub>3</sub>N, HC<sub>5</sub>N, and HC<sub>7</sub>N were determined at the CCSD(T)/cc-pCV5Z level augmented by relativistic corrections computed at the CCSD(T)/cc-pCVQZ level via second-order direct perturbation theory (DPT) [58] and vibrational corrections evaluated using a perturbational approach (VPT2) [59] as described in Ref. [60] for shieldings. Force fields at the MP2/cc-pVTZ level and nuclear quadrupole coupling parameters at the CCSD(T)/cc-pCVTZ level were employed for the vibrational corrections. The <sup>14</sup>N spin-rotation parameters were calculated without further corrections at the CCSD(T)/cc-pCVQZ level. All correlated computations were carried out correlating all electrons. A value of 20.44(3) mb was used for the <sup>14</sup>N nuclear quadrupole moment [61].

All quantum-chemical calculations were carried out using the CFOUR program package [62]; the parallel version of CFOUR was used for some of the calculations [63]. All results of calculations involving the coupled-cluster singles, doubles and triples (CCSDT) [64, 65] and coupled-cluster singles, doubles, triples and quadruples (CCSDTQ) [64, 66] approaches were obtained with the string-based many-body code MRCC [67] interfaced to CFOUR.

The resulting quantum chemically calculated <sup>14</sup>N nuclear quadrupole coupling parameters of HCN to HC<sub>7</sub>N are summarized in Table 5 together with experimental values. The calculated and experimental <sup>14</sup>N nuclear spin-rotation parameters are given in Table 6.

## 6. Discussion of hyperfine parameters

The nuclear quadrupole coupling parameters are usually interpreted in terms of bonding of the respective atom [68, 69]. It is not surprising that the <sup>14</sup>N value of HCN is considerably different from that of HC<sub>3</sub>N (and DC<sub>3</sub>N), as shown in Table 5. Unsurprisingly, the difference is small between HC<sub>3</sub>N and HC<sub>5</sub>N, and very close to zero between HC<sub>5</sub>N and HC<sub>7</sub>N. The calculated non-relativistic equilibrium values differ slightly from the experimental ground state values. The calculated vibrational corrections are modest, of order of one percent. Relativistic corrections are even smaller, as may be expected for a molecule containing only light atoms, but are not negligible at the level with which most of the experimental values have been determined. The agreement between calculated and experimental ground state values is excellent for HC<sub>3</sub>N and DC<sub>3</sub>N and very good for all others. The agreement in the case of HC<sub>7</sub>N needs to be taken with some caution as the uncertainty of the experimental value is one order of magnitude larger than the deviation. Nevertheless, the value of  $-4275$  kHz, determined with keeping the nuclear spin-rotation parameter fixed the value calculated by quantum chemical means, fits the trend better than the

value  $-4299$  kHz without this parameter in the fit, even though both values are compatible within the experimental uncertainties.

The agreement between calculated equilibrium nuclear spin-rotation parameters and the experimental ground state values in Table 6 is very good. The very small deviations for HCN and HC<sub>3</sub>N may well be caused by the neglect of vibrational contributions; their determination could not be carried out with the programs at our disposal.

While the differences between calculated and experimental nuclear quadrupole coupling parameters are relatively small, we note that this is most likely due to error compensation. The computed <sup>14</sup>N nuclear electric quadrupole parameters are found to depend sensitively on the equilibrium structure used. Moreover, they show very slow convergence with respect to basis set size and correlation treatment, which will be discussed in the following.

Although structures obtained at the CCSD(T)/cc-pCVQZ level are quite close to equilibrium structures derived from experiment [57], a shift in the <sup>14</sup>N value of HCN by  $-5.0$  kHz is obtained at the CCSD(T)/cc-pCV5Z level upon going from the CCSD(T)/cc-pCVQZ equilibrium structure ( $r_e(\text{CH}) = 106.554$  pm, and  $r_e(\text{CN}) = 115.384$  pm) to the equilibrium structures derived from experiment ( $r_e(\text{CH}) = 106.501(8)$  pm, and  $r_e(\text{CN}) = 115.324(2)$  pm) [72]. It is assumed that similar deviations would be found if more accurate equilibrium structures would be available for HC<sub>3</sub>N, HC<sub>5</sub>N, and HC<sub>7</sub>N. We would like to emphasize here that these corrections are rather small in relative terms, though not negligible in comparison with experimental accuracy, which is important to realize for the discussion that follows. Furthermore, the uncertainty of the value of the <sup>14</sup>N quadrupole moment (20.44 mb) is  $\pm 0.03$  mb, which translates roughly to 0.15% or values between  $\pm 6.9$  and  $\pm 6.3$  kHz for the molecules under study.

In the cases of HCN and HC<sub>3</sub>N, it was possible to evaluate the equilibrium <sup>14</sup>N values with an even larger basis. Separating the total <sup>14</sup>N value into contributions from Hartree-Fock (HF) and CCSD(T) reveals on the one hand that the HF contribution still changes by  $-12.7$  kHz and  $-12.0$  kHz when increasing the basis set quality from cc-pCV5Z to cc-pCV6Z for HCN and HC<sub>3</sub>N, respectively. On the other hand, the correlation contribution at this level changes from cc-pCV5Z to cc-pCV6Z by less than 1 kHz in the same direction. An equal shift of  $-12.0$  kHz was found for HC<sub>5</sub>N at the HF level by increasing the basis set level from cc-pCV5Z to cc-pCV6Z.

Considering higher-level correlation effects beyond CCSD(T) by employing fc-CCSDT/cc-pVTZ and fc-CCSDTQ/cc-pVDZ computations shows corrections that differ in sign but also in magnitude. The difference between fc-CCSDT/cc-pVTZ and fc-CCSD(T)/cc-pVTZ is found to be  $-10.7$  and  $-13.1$  kHz for HCN and HC<sub>3</sub>N, respectively. However, the corresponding differences between fc-CCSDTQ/cc-pVDZ and fc-CCSDT/cc-pVDZ are found to be about twice as large and positive with values of  $+20.5$  kHz for HCN and  $+24.3$  kHz for HC<sub>3</sub>N.

Although the relativistic corrections obtained at the CCSD(T) level via second-order direct perturbation theory are

Table 5: Quantum chemically calculated non-relativistic equilibrium nuclear electric quadrupole parameters  $eQq(N)_e$  (kHz) of HCN, HC<sub>3</sub>N, DC<sub>3</sub>N, HC<sub>5</sub>N and HC<sub>7</sub>N, relativistic (Rel.) and vibrational (Vib.) corrections, and their sum (kHz) in comparison to experimental ground state parameters and difference O-C (kHz) between experimental and calculated values.

Molecule	$eQq(N)_e^b$	Rel. <sup>c</sup>	Vib. <sup>d</sup>	Sum	Exptl.	O-C
HCN	-4668.9	1.8	-32.2	-4699.4	-4707.83 (6) <sup>e</sup>	-8.4
HC <sub>3</sub> N	-4344.5	3.5	21.0	-4320.0	-4319.24 (1) <sup>f</sup>	0.8
DC <sub>3</sub> N	-4344.5	3.5	22.6	-4318.3	-4318.03 (30) <sup>g</sup>	0.3
HC <sub>5</sub> N	-4326.0	3.6	41.7	-4280.7	-4276.80 (14) <sup>h</sup>	3.9
HC <sub>7</sub> N	-4326.2	3.6	52.3	-4270.3	-4275. (50) <sup>h</sup>	-4.7

<sup>a</sup> All quantum chemical results from this work; CCSD(T)/cc-pCVQZ structural parameters were used; see also section 5 for further details. Sources of experimental data are given separately. Numbers in parentheses of experimental data are one standard deviation in units of the least significant figures.

<sup>b</sup> Calculated at the CCSD(T)/cc-pCV5Z level.

<sup>c</sup> Calculated at the CCSD(T)/cc-pCVQZ level using second-order direct perturbation theory.

<sup>d</sup> Calculated employing MP2/cc-pVTZ for the required force field and CCSD(T)/cc-pCVTZ for the nuclear electric quadrupole parameters.

<sup>e</sup> Ref. [70].

<sup>f</sup> Ref. [71].

<sup>g</sup> Ref. [22].

<sup>h</sup> This work.

relatively small, they are overestimated for all molecules but HCN by about 40% if they are evaluated employing the smaller cc-pCVTZ basis set. In the case of HCN, they are overestimated by about 70% if the smaller basis is employed. However, for HCN the change when going from cc-pCVQZ to cc-pCV5Z is only -0.2 kHz (about 10%).

The vibrational correction obtained using VPT2 at the MP2/cc-pVTZ level for the required force field and at the CCSD(T)/cc-pCVTZ level for the nuclear quadrupole coupling parameters could be improved for HCN to CCSD(T)/cc-pCVQZ for the force field and CCSD(T)/cc-pCV5Z for the nuclear quadrupole coupling, which resulted in a modest change of -0.6 kHz. For HC<sub>3</sub>N/DC<sub>3</sub>N, improved VPT2 computations at the CCSD(T)/cc-pCVTZ level yielded vibrational corrections that are 5.3/5.1 kHz smaller than those reported in Table 5.

Summarizing all the previously mentioned improvements for HCN, a total correction of -9.6 kHz is obtained, which would reduce the difference between observed and calculated from -8.4 kHz to +1.2 kHz. For HC<sub>3</sub>N/DC<sub>3</sub>N total corrections of -6.9/-6.7 kHz would be obtained, while the correction due to the uncertainty in the equilibrium structure remains unknown.

Since the discussed corrections can currently not be applied consistently to all molecules under study, it has to be assumed that similar compensation effects hold for the <sup>14</sup>N nuclear quadrupole coupling parameters of HC<sub>5</sub>N and HC<sub>7</sub>N, which is supported by the *too good* agreement with experiment observed.

With respect to the <sup>14</sup>N spin-rotation parameters, only little variations of the CCSD(T) results are found when increasing the basis set size. When going from cc-pCVQZ to cc-pCV5Z, changes of -0.028 and 0.004 kHz are found for HCN and HC<sub>3</sub>N, respectively. Employing again fc-CCSDT/cc-pVTZ and fc-CCSDTQ/cc-pVDZ computations to estimate the higher-

Table 6: Experimental ground state nuclear magnetic spin-rotation parameters  $C^a$  (kHz) of HC<sub>5</sub>N and HC<sub>7</sub>N in comparison to experimental data for HCN, and HC<sub>3</sub>N and in comparison to equilibrium data from quantum chemical calculations (QCC).

Molecule	Exptl.	QCC
HCN <sup>b</sup>	10.13 (2)	9.938
HC <sub>3</sub> N <sup>c</sup>	0.976 (3)	0.986
HC <sub>5</sub> N <sup>d</sup>	0.2896 (123)	0.290
HC <sub>7</sub> N <sup>e</sup>		0.123

<sup>a</sup> Numbers in parentheses of experimental data are one standard deviation in units of the least significant figures. All quantum chemical results are from this work; calculations at the CCSD(T)/cc-pCVQZ level for both structures and values of  $C$ ; see also section 5. Sources of experimental data are given separately.

<sup>b</sup> Ref. [70].

<sup>c</sup> Ref. [71].

<sup>d</sup> This work.

<sup>e</sup> The value was kept fixed in this work to the value of a quantum chemical calculation; see also Table 3.

level correlation effects in HCN, which has the largest spin-rotation parameter value, changes of +0.022 and -0.029 kHz are found for CCSDT and CCSDTQ, respectively, which almost cancel each other. However, comparing the resulting corrected values of 10.001 kHz (HCN) and 0.990 kHz (HC<sub>3</sub>N) with experiment, only an improvement for the value of HCN is observed, cf. Table 6.

## 7. Conclusions

Accurate transition frequencies of HC<sub>5</sub>N and HC<sub>7</sub>N were determined employing Fourier transform microwave spectroscopy. These data led to improvements of the spectroscopic parameters. In particular, we improved the accuracy of the <sup>14</sup>N nuclear quadrupole coupling parameter of HC<sub>5</sub>N considerably and that of HC<sub>7</sub>N slightly. In addition, we determined for the first time an experimental value of the nuclear <sup>14</sup>N nuclear spin-rotation parameter of HC<sub>5</sub>N. Our quantum chemical calculations were able to reproduce the <sup>14</sup>N hyperfine parameter of HCN to HC<sub>7</sub>N very well. Vibrational corrections to nuclear quadrupole coupling parameters were crucial and relativistic corrections were important to reach nearly the accuracies with which these parameters were determined experimentally. Inclusion of a calculated, very small nuclear spin-rotation value of HC<sub>7</sub>N had a remarkable effect on the value of the nuclear quadrupole coupling parameter. Finally, we pointed out that the HC<sub>5</sub>N rest frequencies may be useful for determining the local speed of rest in dense molecular clouds if these lines are sufficiently strong. Other examples of molecular species with comparatively rich rotational spectra have been mentioned in addition.

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## Appendix A. Supplementary Material

Supplementary data associated with this article can be found, in the online version, at ...

## References

- [1] N. W. Broten, T. Oka, L. W. Avery, J. M. MacLeod, H. W. Kroto, The detection of HC<sub>9</sub>N in interstellar space, *Astrophys. J. Lett.* 223 (1978) L105–L107. doi:10.1086/182739.
- [2] R. A. Loomis, C. N. Shingledecker, G. Langston, B. A. McGuire, N. M. Dollhopf, A. M. Burkhardt, J. Corby, S. T. Booth, P. B. Carroll, B. Turner, A. J. Remijan, Non-detection of HC<sub>11</sub>N towards TMC-1: constraining the chemistry of large carbon-chain molecules, *Mon. Not. R. Astron. Soc.* 463 (2016) 4175–4183. arXiv:1609.02570, doi:10.1093/mnras/stw2302.
- [3] A. M. Burkhardt, E. Herbst, S. V. Kalenskii, M. C. McCarthy, A. J. Remijan, B. A. McGuire, Detection of HC<sub>5</sub>N and HC<sub>7</sub>N isotopologues in TMC-1 with the Green Bank Telescope, *Mon. Not. R. Astron. Soc.* 474 (2018) 5068–5075. arXiv:1711.07495, doi:10.1093/mnras/stx2972.
- [4] K. Taniguchi, M. Saito, First detection of HC<sub>5</sub><sup>15</sup>N in the interstellar medium, *Publ. Astron. Soc. Jpn.* 69 (2017) L7. arXiv:1706.08662, doi:10.1093/pasj/psx065.
- [5] D. R. Schmidt, L. M. Ziurys, Exotic carbon chemistry in a planetary nebula: The unusual case of K4-47, *Astrophys. J. Lett.* 881 (2) (2019) L38. doi:10.3847/2041-8213/ab3663.
- [6] F. Wyrowski, P. Schilke, S. Thorwirth, K. M. Menten, G. Winnewisser, Physical conditions in the proto-planetary nebula CRL 618 derived from observations of vibrationally excited HC<sub>3</sub>N, *Astrophys. J.* 586 (1) (2003) 344–355. arXiv:astro-ph/0211574, doi:10.1086/367637.
- [7] J. R. Pardo, J. Cernicharo, Molecular abundances in CRL 618, *Astrophys. J.* 654 (2) (2007) 978–987. doi:10.1086/509568.
- [8] K. Taniguchi, H. Ozeki, M. Saito, <sup>13</sup>C isotopic fractionation of HC<sub>3</sub>N in two starless cores: L1521B and L134N (L183), *Astrophys. J.* 846 (1) (2017) 46. arXiv:1707.08267, doi:10.3847/1538-4357/aa82ba.
- [9] L. W. Avery, N. W. Broten, J. M. MacLeod, T. Oka, H. W. Kroto, Detection of the heavy interstellar molecule cyanodiacetylene, *Astrophys. J. Lett.* 205 (1976) L173–L175. doi:10.1086/182117.
- [10] L. T. Little, P. W. Riley, D. N. Matheson, Detection of the J = 9-8 transition of interstellar cyanodiacetylene, *Mon. Not. R. Astron. Soc.* 181 (1977) 33P–35P. doi:10.1093/mnras/181.1.33P.
- [11] E. Churchwell, G. Winnewisser, C. M. Walmsley, Molecular observations of a possible proto-solar nebula in a dark cloud in Taurus, *Astron. Astrophys.* 67 (1978) 139–147.
- [12] H. W. Kroto, C. Kirby, D. R. M. Walton, L. W. Avery, N. W. Broten, J. M. MacLeod, T. Oka, The detection of cyanohexatriyne, H(C≡C)<sub>3</sub>CN, in Heile's Cloud 2, *Astrophys. J. Lett.* 219 (1978) L133–L137. doi:10.1086/182623.
- [13] G. Winnewisser, C. M. Walmsley, The detection of HC<sub>5</sub>N and HC<sub>7</sub>N in IRC +10216, *Astron. Astrophys.* 70 (1978) L37–L39.
- [14] M. C. McCarthy, J. U. Grabow, M. J. Travers, W. Chen, C. A. Gottlieb, P. Thaddeus, Laboratory detection of the carbon chains HC<sub>15</sub>N and HC<sub>17</sub>N, *Astrophys. J. Lett.* 494 (2) (1998) L231–L234. doi:10.1086/311188.
- [15] A. J. Alexander, H. W. Kroto, D. R. M. Walton, The microwave spectrum, substitution structure and dipole moment of cyanobutadiyne, H–C≡C–C≡C–C≡N, *J. Mol. Spectrosc.* 62 (2) (1976) 175–180. doi:10.1016/0022-2852(76)90347-7.
- [16] G. Winnewisser, R. A. Creswell, M. Winnewisser, Formation of cyanopolynes in gas discharges, *Z. Naturforsch. A* 33 (1978) 1169–1172. doi:10.1515/zna-1978-1008.
- [17] G. Winnewisser, M. Winnewisser, J. J. Christiansen, The millimeter wave spectrum and discharge chemistry of HC<sub>5</sub>N, *Astron. Astrophys.* 109 (1) (1982) 141–144.
- [18] L. Bizzocchi, C. Degli Esposti, P. Botschwina, Millimeter-wave spectroscopy of rare isotopomers of HC<sub>5</sub>N and DC<sub>5</sub>N: determination of a mixed experimental-theoretical equilibrium structure for cyanobutadiyne, *J. Mol. Spectrosc.* 225 (2) (2004) 145–151. doi:10.1016/j.jms.2004.02.019.
- [19] C. Kirby, H. W. Kroto, D. R. M. Walton, The microwave spectrum of cyanohexatriyne, H–C≡C–C≡C–C≡C–C≡N, *J. Mol. Spectrosc.* 83 (1980) 261–265. doi:10.1016/0022-2852(80)90049-1.
- [20] M. C. McCarthy, E. S. Levine, A. J. Apponi, P. Thaddeus, Experimental structures of the carbon chains HC<sub>7</sub>N, HC<sub>9</sub>N, and HC<sub>11</sub>N by isotopic substitution, *J. Mol. Spectrosc.* 203 (1) (2000) 75–81. doi:10.1006/jmsp.2000.8149.
- [21] L. Bizzocchi, C. Degli Esposti, Laboratory transition frequencies for millimeter-wave lines of vibrationally excited HC<sub>7</sub>N, *Astrophys. J.* 614 (1) (2004) 518–524. doi:10.1086/423370.
- [22] H. Spahn, H. S. P. Müller, T. F. Giesen, J.-U. Grabow, M. E. Harding, J. Gauss, S. Schlemmer, Rotational spectra and hyperfine structure of isotopic species of deuterated cyanoacetylene, DC<sub>3</sub>N, *Chem. Phys.* 346 (1) (2008) 132–138. doi:10.1016/j.chemphys.2007.12.018.
- [23] T. J. Balle, W. H. Flygare, Fabry-Perot cavity pulsed Fourier transform microwave spectrometer with a pulsed nozzle particle source, *Rev. Sci. Instrum.* 52 (1) (1981) 33–45. doi:10.1063/1.1136443.

- [24] J. U. Grabow, W. Stahl, A pulsed molecular beam microwave Fourier transform spectrometer with parallel molecular beam and resonator axes, *Z. Naturforsch. A* 45 (8) (1990) 1043–1044. doi:10.1515/zna-1990-0817.
- [25] J.-U. Grabow, E. S. Palmer, M. C. McCarthy, P. Thaddeus, Supersonic-jet cryogenic-resonator coaxially oriented beam-resonator arrangement Fourier transform microwave spectrometer, *Rev. Sci. Instrum.* 76 (9) (2005) 093106–093106–11. doi:10.1063/1.2039347.
- [26] H. S. P. Müller, A. Coutens, A. Walters, J.-U. Grabow, S. Schlemmer, Rotational spectroscopy, dipole moment and  $^{14}\text{N}$  nuclear hyperfine structure of iso-propyl cyanide, *J. Mol. Spectrosc.* 267 (1-2) (2011) 100–107. arXiv:1102.5675, doi:10.1016/j.jms.2011.02.011.
- [27] H. S. P. Müller, O. Zingsheim, N. Wehres, J.-U. Grabow, F. Lewen, S. Schlemmer, Rotational spectroscopy of the lowest energy conformer of 2-cyanobutane, *J. Phys. Chem. A* 121 (38) (2017) 7121–7129. doi:10.1021/acs.jpca.7b06072.
- [28] H. M. Pickett, The fitting and prediction of vibration-rotation spectra with spin interactions, *J. Mol. Spectrosc.* 148 (2) (1991) 371–377. doi:10.1016/0022-2852(91)90393-0.
- [29] C. P. Endres, S. Schlemmer, P. Schilke, J. Stutzki, H. S. P. Müller, The Cologne Database for Molecular Spectroscopy, CDMS, in the Virtual Atomic and Molecular Data Centre, VAMDC, *J. Mol. Spectrosc.* 327 (2016) 95–104. arXiv:1603.03264, doi:10.1016/j.jms.2016.03.005.
- [30] N. Kaifu, M. Ohishi, K. Kawaguchi, S. Saito, S. Yamamoto, T. Miyaji, K. Miyazawa, S.-I. Ishikawa, C. Noumaru, S. Harasawa, M. Okuda, H. Suzuki, A 8.8–50GHz complete spectral line survey toward TMC-1 I. Survey data, *Publ. Astron. Soc. Jpn.* 56 (2004) 69–173. doi:10.1093/pasj/56.1.69.
- [31] L. Bizzocchi, F. Tamassia, J. Laas, B. M. Giuliano, C. Degli Esposti, L. Dore, M. Melosso, E. Canè, A. Pietropolli Charmet, H. S. P. Müller, H. Spahn, A. Belloche, P. Caselli, K. M. Menten, R. T. Garrod, Rotational and high-resolution infrared spectrum of  $\text{HC}_3\text{N}$ : global rovibrational analysis and improved line catalog for astrophysical observations, *Astrophys. J. Suppl. Ser.* 233 (1) (2017) 11. arXiv:1711.08592, doi:10.3847/1538-4365/aa9571.
- [32] S. Thorwirth, H. S. P. Müller, G. Winnewisser, Millimetre- and submillimetre-wave spectroscopy of  $^{13}\text{C}$  and  $^{15}\text{N}$  isotopomers of cyanoacetylene,  $\text{HCCCN}$ , in the ground and vibrationally excited states, *Phys. Chem. Chem. Phys.* 3 (2001) 1236–1241. doi:10.1039/B009743H.
- [33] G. Cazzoli, C. Pizzarini, Lamb-dip spectrum of methylacetylene and methylidyneacetylene: precise rotational transition frequencies and parameters of the main isotopic species, *Astron. Astrophys.* 487 (3) (2008) 1197–1202. doi:10.1051/0004-6361/200809938.
- [34] G. Cazzoli, C. Pizzarini, The Lamb-dip spectrum of methylcyanide: precise rotational transition frequencies and improved ground-state rotational parameters, *J. Mol. Spectrosc.* 240 (2) (2006) 153–163. doi:10.1016/j.jms.2006.09.013.
- [35] H. S. P. Müller, L. R. Brown, B. J. Drouin, J. C. Pearson, I. Kleiner, R. L. Sams, K. Sung, M. H. Ordu, F. Lewen, Rotational spectroscopy as a tool to investigate interactions between vibrational polyads in symmetric top molecules: Low-lying states  $v_8 \leq 2$  of methyl cyanide,  $\text{CH}_3\text{CN}$ , *J. Mol. Spectrosc.* 312 (2015) 22–37. arXiv:1502.06867, doi:10.1016/j.jms.2015.02.009.
- [36] H. S. P. Müller, B. J. Drouin, J. C. Pearson, Rotational spectra of isotopic species of methyl cyanide,  $\text{CH}_3\text{CN}$ , in their ground vibrational states up to terahertz frequencies, *Astron. Astrophys.* 506 (3) (2009) 1487–1499. arXiv:0910.3111, doi:10.1051/0004-6361/200912932.
- [37] G. Y. Golubiatnikov, A. V. Lapinov, A. Guarnieri, R. Knöchel, Precise Lamb-dip measurements of millimeter and submillimeter wave rotational transitions of  $^{16}\text{O}^{12}\text{C}^{32}\text{S}$ , *J. Mol. Spectrosc.* 234 (1) (2005) 190–194. doi:10.1016/j.jms.2005.08.012.
- [38] G. Y. Golubiatnikov, S. P. Belov, A. V. Lapinov, The accuracy of measurements of the spectral-line frequencies in the studies of the rotational transitions of the  $^{16}\text{O}^{12}\text{C}^{32}\text{S}$  molecule in the millimeter and submillimeter wave ranges, *Radiophys. Quantum Electron.* 58 (8) (2016) 622–631. doi:10.1007/s11141-016-9634-5.
- [39] S. C. Mehrotra, G. Bestmann, H. Dreizler, H. Mäder, A contribution to the investigation of  $T_2$ -relaxation: rotational transitions of  $\text{OCS}$  and  $\text{SO}_2$ , *Z. Naturforsch. A* 39 (7) (1984) 633–636. doi:10.1515/zna-1984-0707.
- [40] S. C. Mehrotra, H. Dreizler, H. Mäder, J-dependence of  $T_2$  parameters for rotational transitions of  $\text{SO}_2$  and  $\text{CH}_3\text{OH}$  in K-band, *Z. Naturforsch. A* 40 (7) (1985) 683–685. doi:10.1515/zna-1985-0705.
- [41] E. A. Alekseev, S. F. Dyubko, V. V. Ilyushin, S. V. Podnos, The high-precision millimeter-wave spectrum of  $^{32}\text{SO}_2$ ,  $^{32}\text{SO}_2$  ( $v_2$ ), and  $^{34}\text{SO}_2$ , *J. Mol. Spectrosc.* 176 (2) (1996) 316–320. doi:10.1006/jmsp.1996.0092.
- [42] H. S. P. Müller, S. Brünken, Accurate rotational spectroscopy of sulfur dioxide,  $\text{SO}_2$ , in its ground vibrational and first excited bending states,  $v_2 = 0, 1$ , up to 2 THz, *J. Mol. Spectrosc.* 232 (2) (2005) 213–222. doi:10.1016/j.jms.2005.04.010.
- [43] A. Maeda, I. R. Medvedev, M. Winnewisser, F. C. De Lucia, E. Herbst, H. S. P. Müller, M. Koerber, C. P. Endres, S. Schlemmer, High-frequency rotational spectrum of thioformaldehyde,  $\text{H}_2\text{CS}$ , in the ground vibrational state, *Astrophys. J. Suppl. Ser.* 176 (2) (2008) 543–550. doi:10.1086/528684.
- [44] H. S. P. Müller, A. Maeda, S. Thorwirth, F. Lewen, S. Schlemmer, I. R. Medvedev, M. Winnewisser, F. C. De Lucia, E. Herbst, Laboratory spectroscopic study of isotopic thioformaldehyde,  $\text{H}_2\text{CS}$ , and determination of its equilibrium structure, *Astron. Astrophys.* 621 (2019) A143. arXiv:1812.01554, doi:10.1051/0004-6361/201834517.
- [45] H. S. P. Müller, K. M. Menten, H. Mäder, Accurate rest frequencies of methanol maser and dark cloud lines, *Astron. Astrophys.* 428 (2004) 1019–1026. arXiv:astro-ph/0408094, doi:10.1051/0004-6361:20041384.
- [46] L. H. Coudert, C. Gutlé, T. R. Huet, J.-U. Grabow, S. A. Levshakov, Spin-torsion effects in the hyperfine structure of methanol, *J. Chem. Phys.* 143 (4) (2015) 044304. doi:10.1063/1.4926942.
- [47] R. J. Bartlett, M. Musiał, Coupled-cluster theory in quantum chemistry, *Rev. Mod. Phys.* 79 (2007) 291–352. doi:10.1103/RevModPhys.79.291.
- [48] K. Raghavachari, G. W. Trucks, J. A. Pople, M. Head-Gordon, A fifth-order perturbation comparison of electron correlation theories, *Chem. Phys. Lett.* 157 (6) (1989) 479–483. doi:10.1016/S0009-2614(89)87395-6.
- [49] G. E. Scuseria, Analytic evaluation of energy gradients for the singles and doubles coupled cluster method including perturbative triple excitations: Theory and applications to FOOF and  $\text{Cr}_2$ , *J. Chem. Phys.* 94 (1) (1991) 442–447. doi:10.1063/1.460359.
- [50] J. D. Watts, J. Gauss, R. J. Bartlett, Open-shell analytical energy gradients for triple excitation many-body, coupled-cluster methods: MBPT(4), CCSD+T(CCSD), CCSD(T), and QCISD(T), *Chem. Phys. Lett.* 200 (1) (1992) 1–7. doi:10.1016/0009-2614(92)87036-0.
- [51] J. Gauss, J. F. Stanton, Perturbative treatment of triple excitations in coupled-cluster calculations of nuclear magnetic shielding constants, *J. Chem. Phys.* 104 (7) (1996) 2574–2583. doi:10.1063/1.471005.
- [52] T. H. Dunning, Jr., Gaussian basis sets for use in correlated molecular calculations. I. The atoms boron through neon and hydrogen, *J. Chem. Phys.* 90 (2) (1989) 1007–1023. doi:10.1063/1.456153.
- [53] D. E. Woon, T. H. Dunning, Jr., Gaussian basis sets for use in correlated molecular calculations. V. Core-valence basis sets for boron through neon, *J. Chem. Phys.* 103 (11) (1995) 4572–4585. doi:10.1063/1.470645.
- [54] A. K. Wilson, T. van Mourik, T. H. Dunning, Gaussian basis sets for use in correlated molecular calculations. VI. Sextuple zeta correlation consistent basis sets for boron through neon, *J. Mol. Struct.: THEOCHEM* 388 (1996) 339–349. doi:10.1016/S0166-1280(96)80048-0.
- [55] J. Gauss, K. Ruud, T. Helgaker, Perturbation-dependent atomic orbitals for the calculation of spin-rotation constants and rotational  $g$  tensors, *J. Chem. Phys.* 105 (7) (1996) 2804–2812. doi:10.1063/1.472143.
- [56] J. Gauss, D. Sundholm, Coupled-cluster calculations of spin-rotation constants, *Mol. Phys.* 91 (3) (1997) 449–458. doi:10.1080/002689797171346.
- [57] K. L. Bak, J. Gauss, P. Jørgensen, J. Olsen, T. Helgaker, J. F. Stanton, The accurate determination of molecular equilibrium structures, *J. Chem. Phys.* 114 (15) (2001) 6548–6556. doi:10.1063/1.1357225.
- [58] S. Stopkowicz, J. Gauss, Relativistic corrections to electrical first-order properties using direct perturbation theory, *J. Chem. Phys.* 129 (16) (2008) 164119. doi:10.1063/1.2998300.
- [59] I. M. Mills, Vibrationally averaged interatomic distances, *J. Chem. Phys.* 80 (11) (1976) 1187–1188. doi:10.1021/j100552a013.
- [60] A. A. Auer, J. Gauss, J. F. Stanton, Quantitative prediction of gas-phase

- $^{13}\text{C}$  nuclear magnetic shielding constants, *J. Chem. Phys.* 118 (23) (2003) 10407–10417. doi:10.1063/1.1574314.
- [61] M. Tokman, D. Sundholm, P. Pyykkö, J. Olsen, The nuclear quadrupole moment of  $^{14}\text{N}$  obtained from finite-element MCHF calculations on  $\text{N}^{2+}$  ( $2p$ ;  $^2P_{3/2}$ ) and  $\text{N}^+$  ( $2p^2$ ;  $^3P_2$  and  $2p^2$ ;  $^1D_2$ ), *Chem. Phys. Lett.* 265 (1) (1997) 60–64. doi:10.1016/S0009-2614(96)01433-9.
- [62] J. F. Stanton, J. Gauss, L. Cheng, M. E. Harding, D. A. Matthews, P. G. Szalay, CFOUR, Coupled-Cluster techniques for Computational Chemistry, a quantum-chemical program package, With contributions from A.A. Auer, R.J. Bartlett, U. Benedikt, C. Berger, D.E. Bernholdt, Y.J. Bomble, O. Christiansen, F. Engel, R. Faber, M. Heckert, O. Heun, M. Hilgenberg, C. Huber, T.-C. Jagau, D. Jonsson, J. Jusélius, T. Kirsch, K. Klein, W.J. Lauderdale, F. Lipparini, T. Metzroth, L.A. Mück, D.P. O'Neill, D.R. Price, E. Prochnow, C. Puzzarini, K. Ruud, F. Schiffmann, W. Schwalbach, C. Simmons, S. Stopkowicz, A. Tajti, J. Vázquez, F. Wang, J.D. Watts and the integral packages MOLECULE (J. Almlöf and P.R. Taylor), PROPS (P.R. Taylor), ABACUS (T. Helgaker, H.J. Aa. Jensen, P. Jørgensen, and J. Olsen), and ECP routines by A. V. Mitin and C. van Wüllen. For the current version, see <http://www.cfour.de>.
- [63] M. E. Harding, T. Metzroth, J. Gauss, A. A. Auer, Parallel calculation of CCSD and CCSD(T) analytic first and second derivatives, *J. Chem. Theory Comput.* 4 (2008) 64–74. doi:10.1021/ct700152c.
- [64] M. Kállay, J. Gauss, P. G. Szalay, Analytic first derivatives for general coupled-cluster and configuration interaction models, *J. Chem. Phys.* 119 (6) (2003) 2991–3004. doi:10.1063/1.1589003.
- [65] J. Gauss, Analytic second derivatives for the full coupled-cluster singles, doubles, and triples model: nuclear magnetic shielding constants for BH, HF, CO,  $\text{N}_2$ ,  $\text{N}_2\text{O}$ , and  $\text{O}_3$ , *J. Chem. Phys.* 116 (12) (2002) 4773–4776. doi:10.1063/1.1462612.
- [66] M. Kállay, J. Gauss, Analytic second derivatives for general coupled-cluster and configuration-interaction models, *J. Chem. Phys.* 120 (15) (2004) 6841–6848. doi:10.1063/1.1668632.
- [67] M. Kállay, P. R. Nagy, Z. Rolik, D. Mester, G. Samu, J. Csontos, J. Csóka, B. P. Szabó, L. Gyevi-Nagy, I. Ladjánszki, L. Szegedy, B. Ladóczki, K. Petrov, M. Farkas, P. Mezei, B. Hégyel, MRCC, a quantum chemical program., see also Z. Rolik, L. Szegedy, I. Ladjánszki, B. Ladóczki, and M. Kállay, *J. Chem. Phys.* 139 (2013) 094105; as well as: [www.mrcc.hu](http://www.mrcc.hu).
- [68] B. P. Dailey, C. H. Townes, The ionic character of diatomic molecules, *J. Chem. Phys.* 23 (1) (1955) 118–123. doi:10.1063/1.1740508.
- [69] S. E. Novick, Extended Townes-Dailey analysis of the nuclear quadrupole coupling tensor, *J. Mol. Spectrosc.* 267 (1-2) (2011) 13–18. doi:10.1016/j.jms.2011.01.004.
- [70] W. L. Ebenstein, J. S. Muentner, Dipole moment and hyperfine properties of the ground state and the C-H excited vibrational state of HCN, *J. Chem. Phys.* 80 (9) (1984) 3989–3991. doi:10.1063/1.447269.
- [71] R. L. DeLeon, J. S. Muentner, Molecular beam electric resonance study of the ground and excited states of cyanoacetylene, *J. Chem. Phys.* 82 (4) (1985) 1702–1704. doi:10.1063/1.448402.
- [72] S. Carter, I. M. Mills, N. C. Handy, The equilibrium structure of HCN, *J. Chem. Phys.* 97 (2) (1992) 1606–1607. doi:10.1063/1.463237.